Lecture 3: Overview of Deep Learning System
CSE599G1: Spring 2017
The Deep Learning Systems Juggle

We won't focus on a specific one, but will discuss the common and useful elements of these systems
We will have lectures on each of the parts!
Typical Deep Learning System Stack

User API

- Programming API
- Gradient Calculation (Differentiation API)
- Computational Graph Optimization and Execution
- Runtime Parallel Scheduling
- GPU Kernels, Optimizing Device Code
- Accelerators and Hardwares
Example: Logistic Regression

Data

\[ x_i = \begin{bmatrix}
\text{pixel}_1 \\
\text{pixel}_2 \\
\vdots \\
\text{pixel}_m \\
\end{bmatrix} \]

Fully Connected Layer

\[ h_k = w_k^T x_i \]

Softmax

\[ P(y_i = k | x_i) = \frac{\exp(h_k)}{\sum_{j=1}^{10} \exp(h_j)} \]
Logistic Regression in Numpy

```
import numpy as np
from tinyflow.datasets import get_mnist

def softmax(x):
    x = x - np.max(x, axis=1, keepdims=True)
    x = np.exp(x)
    x = x / np.sum(x, axis=1, keepdims=True)
    return x

# get the mnist dataset
mnist = get_mnist(flatten=True, onehot=True)
learning_rate = 0.5 / 100
W = np.zeros((784, 10))
for i in range(1000):
    batch_xs, batch_ys = mnist.train.next_batch(100)
    # forward
    y = softmax(np.dot(batch_xs, W))
    # Backward
    y_grad = y - batch_ys
    W_grad = np.dot(batch_xs.T, y_grad)
    # update
    W = W - learning_rate * W_grad
```

Forward computation:
Compute probability of each class $y$ given input

- Matrix multiplication
  - $\text{np.dot}(\text{batch}_x, W)$
- Softmax transform the result
  - $\text{softmax}(\text{np.dot}(\text{batch}_x, W))$
Logistic Regression in Numpy

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Manually calculate the gradient of weight with respect to the log-likelihood loss.

Exercise: Try to derive the gradient rule by yourself.
Logistic Regression in Numpy

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```

Weight Update via SGD

$$ w \leftarrow w - \eta \nabla_w L(w) $$
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Discussion: Numpy based Program

- Talk to your neighbors 2-3 person:)
- What do we need to do to support deeper neural networks
- What are the complications
Logistic Regression in Numpy

- Computation in Tensor Algebra
  - $\text{softmax(np.dot(batch\_xs, W))}$

- Manually calculate the gradient
  - $y\_grad = y - batch\_ys$
  - $W\_grad = \text{np.dot(batch\_xs.T, y\_grad)}$

- SGD Update Rule
  - $W = W - \text{learning\_rate} \times W\_grad$
import tinyflow as tf
from tinyflow.datasets import get_mnist

# Create the model
x = tf.placeholder(tf.float32, [None, 784])
W = tf.Variable(tf.zeros([784, 10]))
y = tf.nn.softmax(tf.matmul(x, W))

# Define loss and optimizer
y_ = tf.placeholder(tf.float32, [None, 10])
cross_entropy = tf.reduce_mean(-tf.reduce_sum(y_ * tf.log(y), reduction_indices=[1]))

# Update rule
learning_rate = 0.5
W_grad = tf.gradients(cross_entropy, [W])[0]
train_step = tf.assign(W, W - learning_rate * W_grad)

# Training Loop
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Logistic Regression in TinyFlow

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Automatic Differentiation: Details in next lecture!
Logistic Regression in TinyFlow

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SGD update rule
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```

Real execution happens here!
The Declarative Language: Computation Graph

- Nodes represents the computation (operation)
- Edge represents the data dependency between operations

Computational Graph for \( a \times b + 3 \)
Computational Graph Construction by Step

\[ x = \text{tf.placeholder}(\text{tf.float32}, [\text{None}, 784]) \]

\[ W = \text{tf.Variable}(\text{tf.zeros}([784, 10])) \]

\[ y = \text{tf.nn.softmax}(\text{tf.matmul}(x, W)) \]
Computational Graph by Steps

\[
y_\_ = \text{tf.placeholder}(\text{tf.float32}, [\text{None, 10}])
\]

\[
cross\_entropy = \text{tf.reduce\_mean}(-\text{tf.reduce\_sum}(y\_ \* \text{tf.log}(y), \text{reduction\_indices}=[1]))
\]
Computational Graph Construction by Step

\[ W_{\text{grad}} = \text{tf.gradients}(\text{cross}_\text{entropy}, [W])[0] \]

Automatic Differentiation, detail in next lecture!
Computational Graph Construction by Step

\[
\text{train\_step} = \text{tf.assign}(W, W - \text{learning\_rate} \times W\_\text{grad})
\]
Execution only Touches the Needed Subgraph

```
function sess.run(train_step, feed_dict={x: batch_xs, y_: batch_ys})
```

[Diagram of the computation graph with nodes and edges representing operations such as assign, sub, mul, matmult, softmax, log, log-grad, softmax-grad, mean, and cross_entropy.]
Discussion: Computational Graph

- What is the benefit of computational graph?
- How can we deploy the model to mobile devices?
Discussion: Numpy vs TinyFlow Program

What is the benefit/drawback of the TinyFlow model vs Numpy Model

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Typical Deep Learning System Stack

**System Components**

- Programming API
- Gradient Calculation (Differentiation API)
- Computational Graph Optimization and Execution
- Runtime Parallel Scheduling
- GPU Kernels, Optimizing Device Code
- Accelerators and Hardwares
Computation Graph Optimization

- E.g. Deadcode elimination
- Memory planning and optimization (lecture on Apr 18th)
- What other possible optimization can we do given a computational graph?
Parallel Scheduling

- Code need to run parallel on multiple devices and worker threads
- Detect and schedule parallelizable patterns
- Detail lecture on Apr 25th

MXNet Example

```python
>>> import mxnet as mx
>>> A = mx.nd.ones((2,2)) * 2
>>> C = A + 2
>>> B = A + 1
>>> D = B * C
```
Typical Deep Learning System Stack

Programming API
Gradient Calculation (Differentiation API)

Computational Graph Optimization and Execution
Runtime Parallel Scheduling

GPU Kernels, Optimizing Device Code
Accelerators and Hardwares

Architecture
GPU Acceleration

- Most existing deep learning programs run on GPUs
- Modern GPU have Teraflops of computing power
Custom Hardwares are coming

- Joint Session with CSE 548 on ASIC and FPGA
  - Different date as normal hour
  - Checkout the schedule page for details
Typical Deep Learning System Stack

Not a comprehensive list of elements
The systems are still rapidly evolving :)

**User API**
- Programming API
- Gradient Calculation (Differentiation API)

**System Components**
- Computational Graph Optimization and Execution
- Runtime Parallel Scheduling

**Architecture**
- GPU Kernels, Optimizing Device Code
- Accelerators and Hardwares
Links

- TinyFlow: 2K lines of code to build a TensorFlow like API
  - https://github.com/dlsys-course/tinyflow

- The source code used in the slide
  - https://github.com/dlsys-course/examples/tree/master/lecture3